Calculus Math Curriculum



Egg Harbor Township School District

State Board Adoption Date of Standards: 5/2016

Unit Overview (Standards Coverage)							
Unit	Standards	Unit Focus	Standards for Mathematical Practice	Open Educational Resources			
Unit 1 Limits and Continuity 20 Days	Limits Continuity	How does knowing the value of a limit, or that a limit does not exist, help you to make sense of interesting features of functions and their graphs?	MP.1 Determine expressions and values using mathematical procedures and rules.	AP Central Khan Academy Wolfram Mathworld Delta Math			
Unit 2 Differentiation 50 Days	Differentiation Continuity and Differentiability Rules of Differentiation Applications of Derivatives	What is meant by an instantaneous rate of change? How do mathematical properties and rules for simplifying and evaluating limits apply to differentiation?	MP.2 Translate mathematical information from a single representation or across multiple representations.	AP Central Khan Academy Wolfram Mathworld Delta Math			
Unit 3 Integration 50 Days	Area Integration Differential Equations Applications of Integration	How is integrating to find areas related to differentiating to find slopes?	MP.3 Justify reasoning and solutions. MP.4 Use correct notation,	AP Central Khan Academy Wolfram Mathworld Delta Math			
			language, and mathematical conventions to communicate results or solutions.				

This document outlines in detail the answers to following four questions:

- 1. What do we want our students to know?
 - 2. How do we know if they learned it?
- 3. What do we do if they did not learn it?
- 4. What do we do when they did learn it?

Unit 1 CALCULUS: Limits and Continuity						
Content & Practice Standards			Critical Knowledge & Skills			
 Limits Continuity Asymptotes 	Reading: Infused within the unit are connections of NJSLS for Mathematics, Language Arts Literacy WHST.11-12.10. Write routinely over extended time frames (time for reflection and revision) and shorted time frames (a single sitting or a day or two) for a most of discipline-specific tasks, purposes, and audiences. Educational Technology: All students will use digit tools to access, manage, evaluate, and synthesize information in order to solve problems individually collaborate and to create and communicate knowledge.		Students will solve for Limits, Continuity and Asymptotes.			
		LUS: Limits and Continuity				
Stage 1 – Desired Results						
UNIT SUMMARY Students must understand the concept of limits before proce differentiation. We learn to interpret functions graphically, analytically, and verbally.		 CORE AND SUPPLEMENTAL MATERIALS/RESOURCES Textbook TI-89 Graphing Calculator 				
	Un	DERSTANDINGS				
Students will understand there may be a difference between the value of a function at a given point and the limit of that function as <i>x</i> approaches the given point. Students will understand that mathematical information can be presented graphically, numerically, analytically, and/or verbally.						
Students will know		Students will be able to				
What is meant by the concepts of limits and continuity. How to evaluate/estimate limits graphically, numerically, and analytically.		Evaluate/estimate limits graphically, numerically, and analytically. Use appropriate notation for limits.				
Stage 2 – Assessment Evidence						
Performance Tasks: What projects, hands-on lessons, use of manipulatives, active participation in new situations, etc. will reveal evidence of meaning-making and transfer (true understanding)? Performance Tasks/Use of Technology Khan Academy Delta Math College Board		Other Evidence: What other means of assessment will be used throughout this unit? Formative Observation Homework Class Participation Notebook Checks Self-assessment				

Summative

- Chapter/Unit Test
- Quizzes
- Presentations
- Unit Projects

Stage 3 – Learning Plan

Introducing Calculus: Can Change Occur at an Instant?

Defining Limits and Using Limit Notation

Estimating Limit Values from Graphs and Tables

Determining Limits Algebraically

Selecting Procedures for Determining Limits

Determining Limits Using the Squeeze Theorem

Connecting Multiple Representations of Limits

Defining Continuity at a Point and Over an Interval

Connecting Limits and Asymptotes

Planned Differentiation & Interventions for Tiers I, II, III, ELL, SPED, and Gift & Talented Students

- Rethink and revise. Dig deeper into ideas at issue (through the faces of understanding). Revise, rehearse, and refine, as needed. Guide students in self-assessment and self-adjustment, based on feedback from inquiry, results, and discussion.
- Evaluate understandings. Reveal what has been understood through final performances and products. Involve students in a final self-assessment to identify remaining questions, set future goals, and point toward new units and lessons.
- •Tailor (personalize) the work to ensure maximum interest and achievement. Differentiate the approaches used and provide sufficient options and variety (without compromising goals) to make it most likely that all students will be engaged and effective.

Gifted & Talented:

- "Differentiating the Lesson" in Big Ideas online resources for all sections
- "Additional Topics" in Big Ideas online resources to extend and enhance instruction
- Big Ideas Game Closet
- Big Ideas Differentiated Instruction options
- Big Ideas Mini-Assessments
- Design Challenges

- Student Choice/Driven Activities
- Group Projects
- MobyMax
- LinkIt!
- Rocket Math
- <u>Intervention Central</u>
- Do to Learn
- Differentiation Strategies for Math
- Discovery Education Math
- Everyday Mathematics
- Homework Spot
- Math Fact Fluency

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- Vocabulary Support Glossary resources
- Mini-Assessments
- Game Closet
- Lesson Tutorials
- Flash Cards
 - Extended Time
- Flexible Grouping
- Small Group Instruction
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- Learning Ally
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- Discovery Education Math
- Everyday Mathematics
- Homework Spot
- Flash Card Math
- Math Fact Fluency

Tier II:

- Lesson Tutorials
- Basic Skills Handbook
- Skills Review Handbook
- Differentiated Instruction Big Ideas resources
- Game Closet
- Centers/Small Group Instruction
- Math Tutoring Center (HS only)
- Math Lab/Tutorial
- MobyMax
- LinkIt!
- Math Fact Fluency/Rocket Math

Tier III:

- Customized Learning Intervention Activities resources
- Intensive Intervention resource
- Systematic Assessments to focus on specific deficits

ELL:

- Big Ideas Math Student Editions are available online in Spanish
- Letters to Parents are available in the Resources by Chapter book to assist in guiding parents through each chapter and offer helpful suggestions they can use to demonstrate mathematical concepts for their child in daily activities. These letters are editable so teachers can customize them.
- Student Dynamic eBook Audio has the option to be read in English or Spanish
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- Vocabulary Flash Cards
- Chunking Information

- Math Word Wall/Word Bank
- Multi-Sensory Instruction
- Use of Translation software
- Gradual Release Model
- TODOS: Mathematics for ALL Excellence and Equity in Mathematics
- FABRIC A Learning Paradigm for ELLs (NJDOE resource)

SPED:

- Menu Math (mostly for very low functioning students)
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- MobyMax
- LinkIt!
- IXL
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- Apex Online Learning Bridge students only
- Use of specialized equipment such as beeping balls, text to speech and speech to text software, special seats or desks
- Use of hands-on materials for problem solving
- Visual supports and Use of Manipulatives
- Extended time to complete tests and assignments
- Graphic Organizers/Study Guides
- Mnemonic tricks to improve memory
- Reducing workload
- Centers/Small Group Instruction
- Adjusting accountability for standards by focusing only on essential standards
- Use of IPads or laptops for students with motor issues that make writing difficult
- Use of tangible rewards (certificates, small toys, etc. per behavior plan)
- Use prompts and model directions
- Use task analysis to break down activities and lessons into each individual step needed to complete the task
- Use concrete examples to teach concepts
- Have student repeat/rephrase written directions
- Provide multi-sensory, hands-on materials for instruction
- Chunking Information
- Modify all fine motor tasks for example: (fat crayons, pencil grip, adaptive scissors)
- Functional or practical emphasis

504:

- Learning Ally (audio version for textbooks and other published materials)
- Extra help opportunities

- Reduce workload
- Partial credit
- Allow use of calculator, when appropriate
- Modified length and time frame of assignments
- Alternate assessments with extended time
- Provide guided notes and study guides as needed (use interactive notebook)
- Preferential Seating
- Extra Practice
- Directions repeated, clarified and reworded
- Breakdown task into manageable units
- Differentiated instruction
- Use of manipulatives

Unit 2 CALCULUS: Differentiation					
Content & Practice Standards	tent & Practice Standards Interdisciplinary Standards		Critical Knowledge & Skills		
 Differentiation Continuity and Differentiability Rules of Differentiation Applications of Derivatives 	NJSLS for Mathem WHST.11-12.10. W frames (time for retime frames (a sing of discipline-specifi Educational Technology to access, man information in order	within the unit are connections to the natics, Language Arts Literacy rite routinely over extended time flection and revision) and shorter le sitting or a day or two) for a range c tasks, purposes, and audiences. ology: All students will use digital tage, evaluate, and synthesize er to solve problems individually and create and communicate knowledge.	Students must understand and apply differentiation, continuity, differentiability, rules of differentiation and application of derivatives.		
		CULUS: Differentiation			
	Stage	1 – Desired Results			
We solve the tangent line problem and learn that the instanta is equivalent to the slope of the tangent line. We learn that tangent line is dependent on the <i>x</i> -value, and is therefore a fit to learn algebraic methods of finding derivatives, and exploit beyond the slope.	the slope of the function. We proceed	Textbook TI-89 Graphing Calculator			
		DERSTANDINGS			
Students will understand that the slope of the tangent line is equivalent to the instantaneous rate of change. Students will understand that the slope of a curve at a point is a function of the <i>x</i> -value at that point. Students will understand that the derivative can be used to gain additional information about the behavior of the function.					
Students will know		Students will be able to			
Limit Definition of Derivative Power Rule; Product Rule; Quotient Rule; Chain Rule Derivatives of Trig functions and Exponential Functions Higher-Order Derivatives		Evaluate Derivatives Evaluate Derivatives of functions defined implicitly Solve related rates problems			
Stage 2 – Assessment Evidence					
Performance Tasks/Use of Technology Khan Academy Delta Math College Board		Other Evidence: Formative Observation Homework Class Participation Notebook Checks			

Self-assessment

Summative

- Chapter/Unit Test
- Quizzes
- Presentations
- Unit Projects

Stage 3 – Learning Plan

Define Average and Instantaneous Rate of Change

Define Derivative and Derivative Notation

Derivatives of Polynomial; Trigonometric; Exponential Functions

Power Rule; Product Rule; Quotient Rule; Chain Rule

Higher-Order Derivatives

Using Derivatives to solve problems: Related Rates

Using Derivatives to sketch curves

Planned Differentiation & Interventions for Tiers I, II, III, ELL, SPED, and Gift & Talented Students

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- Big Ideas Mini-Assessments

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Tier II:

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- Skills Review Handbook
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Unit 3 CALCULUS: Integration						
Content & Practice Standards Interdisciplinary Star		ndards	Critical Knowledge & Skills			
 Accumulation of Change Anti-differentiation Fundamental Theorem of Calculus Techniques of Integration Applications of Integration Differential Equations 	Reading: Infused within the unit are connections to the NJSLS for Mathematics, Language Arts Literacy WHST.11-12.10. Write routinely over extended time frames (time for reflection and revision) and shorter time frames (a single sitting or a day or two) for a range of discipline-specific tasks, purposes, and audiences. Educational Technology: All students will use digital tools to access, manage, evaluate, and synthesize information in order to solve problems individually and collaborate and to create and communicate knowledge. Unit 3 CALCULUS		Students will utilize and apply Accumulation of Change, anti-differentiation, Fundamental Theorem of Calculus, Techniques of Integration, Applications of Integration and Differential Equations.			
	Stage	1 – Desired Results				
UNIT SUMMARY		CORE AND SUPPLEMENTAL MATE	RIALS/RESOURCES			
We approximate accumulated change with Riemann sums, a process to calculate actual change. We learn the relationshi accumulated change and the anti-derivative, and the Fundar Calculus. We then explore different techniques of integratio integration. We use integration to solve differential equation unusual regions, and to find volumes of solids.	p between mental Theorem of on and applications of	 Textbook TI-89 Graphing Calculator 				
	Un	DERSTANDINGS				
Students will understand that the anti-derivative is not a function of <i>x</i> , but rather a family of functions of <i>x</i> . Students will understand that accumulation of change is related to the area under the curve. Students will understand that a differential equation relates a function of an independent variable to its derivatives.						
Students will know		Students will be able to				
Approximating area using Riemann sums. Integration of polynomial, trigonometric, exponential and logarithmic functions. Integration by substitution. The Fundamental Theorem of Calculus. Solving Differential Equations. Volumes of solids of rotation.		Find the area under a curve. Find definite and indefinite integrals. Solve Differential Equations. Find Volumes of solids of rotation.				
Stage 2 – Assessment Evidence						
Performance Tasks:		Other Evidence: What other means of assessment will be used throughout this unit?				

What projects, hands-on lessons, use of manipulatives, active participation in new situations, etc. will reveal evidence of meaning-making and transfer (true understanding)?

Performance Tasks/Use of Technology

- Khan Academy
- Delta Math
- College Board

Formative

- Observation
- Homework
- Class Participation
- Notebook Checks
- Self-assessment

Summative

- Chapter/Unit Test
- Quizzes
- Presentations
- Unit Projects

Stage 3 – Learning Plan

Introduce accumulation of change and area under a curve

Apply the limit process to Riemann Sum approximation to find exact areas

The Fundamental Theorem of Calculus

The substitution technique for integration

Rules of Integration: polynomial; trigonometric; exponential; logarithmic

Differential Equations

Volumes of solids of rotation

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